

**Analysing Surface Atmospheric Forcing Distributions and Potential Extreme Events**  
Ghani, Mahmud Hasan and Pinardi, Nadia  
Department of Physics and Astronomy, University of Bologna

**Introduction**

The analysis of the probability distributions of atmospheric variables is a significant step in understanding ocean forecasts and minimizing associated uncertainties. The study has investigated the characteristics of density distributions using high-resolution atmospheric model forecast analysis data (ECMWF). After removing the seasonal cycles from 15-years time-series, the transformed anomaly dataset of surface atmospheric variables- wind components (U, V), wind amplitude, air temperature (T2M), dew point temperature (D2M), and mean sea-level pressure (MSL-P) are analyzed with probability distribution functions (PDFs). The distribution parameters are estimated with the Maximum Likelihood Estimate (MLE) method.

The study reveals that a three-parameter skew-normal PDF captures the variance and asymmetric tails (skewness) well. It is found that the PDF parameters vary largely between different regions, both the shape (connected to the asymmetric tails) and the scale (connected to the spread of the distribution). Potential extreme values, 95th and 5th percentiles, are computed from the inverse Cumulative Density Function (CDF).

**Dataset and Methodology**

**ECMWF analysis dataset:** -spatial resolution 0.125 degree, daily mean resolution (converted from 6-hourly)  
**Observed variables:** D2M, T2M, MSL-P, U10M, V10M

Pre-processing:

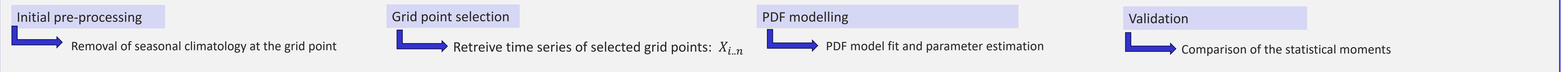
$$\text{Seasonal Climatology (Ct)} = \frac{1}{N} \sum_{j=1}^N X_{t,j} \quad (1) \quad \text{Anomalies } (\bar{X}) = X_t - C_t \quad (2)$$

**PDF models :**

The Weibull PDF (3) comprises shape and scale parameters, and the support is  $x > 0, +\infty$ . The Skew-normal PDF (4) has shape parameter,  $\alpha$ , location parameter,  $\mu$ , and scale parameter,  $\lambda$ , and its support is  $x \in (-\infty, +\infty)$ .

$$f(x; k, \lambda) = \frac{k}{\lambda} \left(\frac{x}{\lambda}\right)^{k-1} \exp\left(-\left(\frac{x}{\lambda}\right)^k\right) \quad (3) \quad f(x; \alpha, \mu, \lambda) = \frac{2}{\lambda} \phi\left(\frac{x-\mu}{\lambda}\right) \Phi\left(\frac{\alpha(x-\mu)}{\lambda}\right) \quad (4)$$

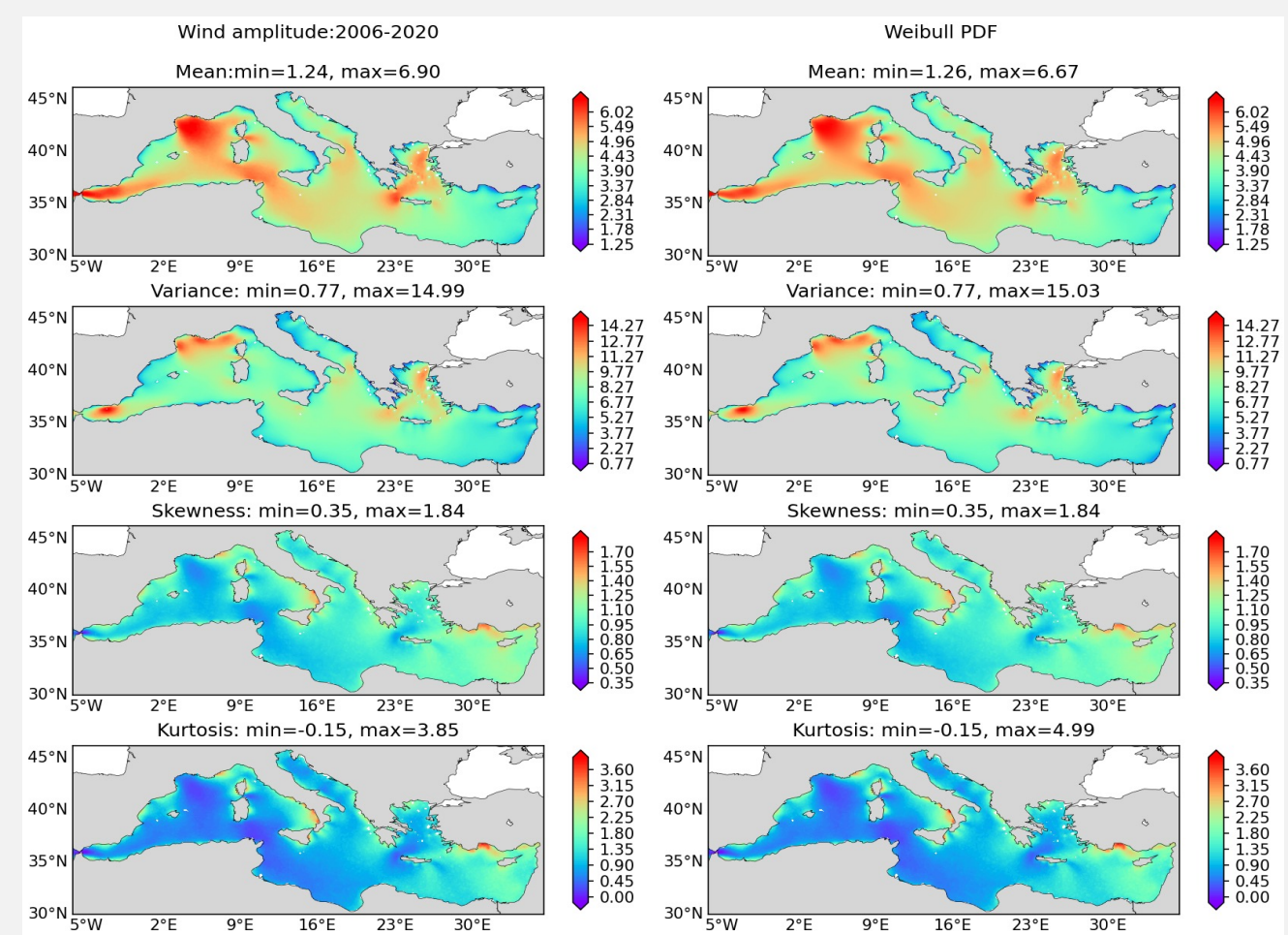
**Schematic diagram of the tool:**



**Weibull PDF fit on wind amplitude**

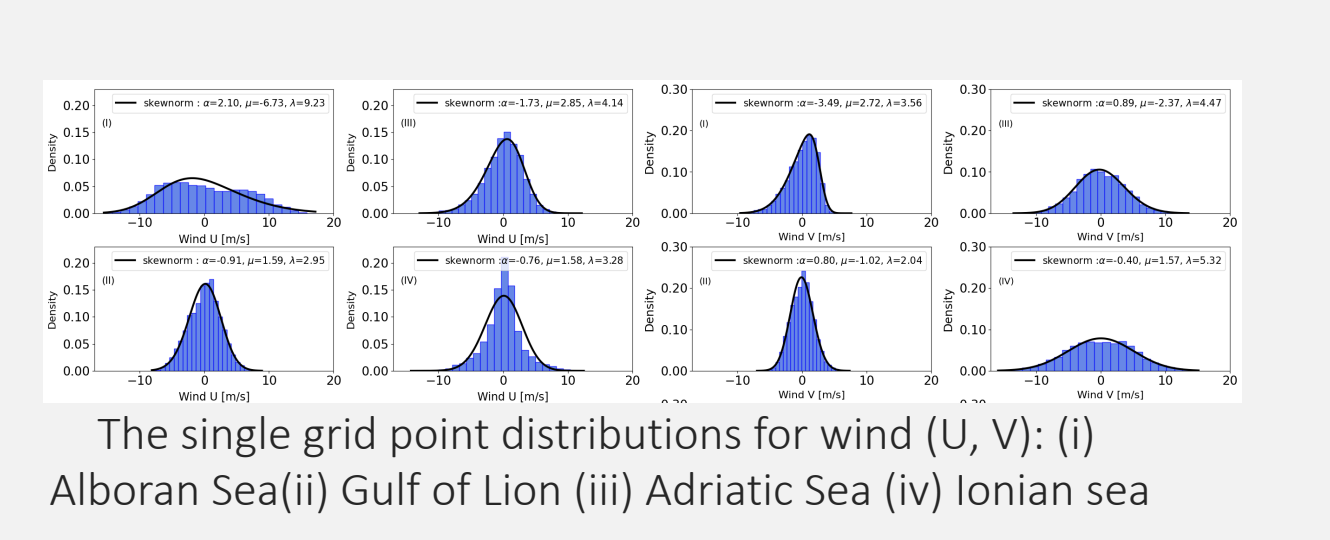
Anomaly of wind amplitude, W is defined as

$$W = \sqrt{(U - \bar{U})^2 + (V - \bar{V})^2} \quad (5)$$

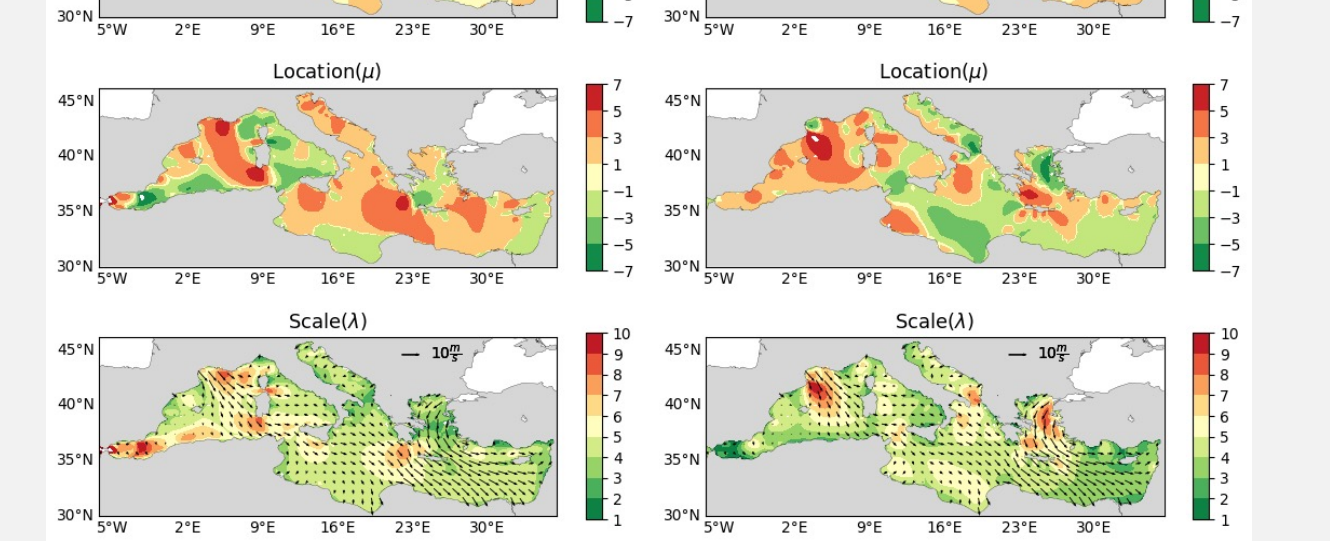


Distributions of the statistical moments (from top to bottom: mean, variance, skewness, kurtosis): left panel estimated from anomaly data, right panel estimated from Weibull fitted distributions

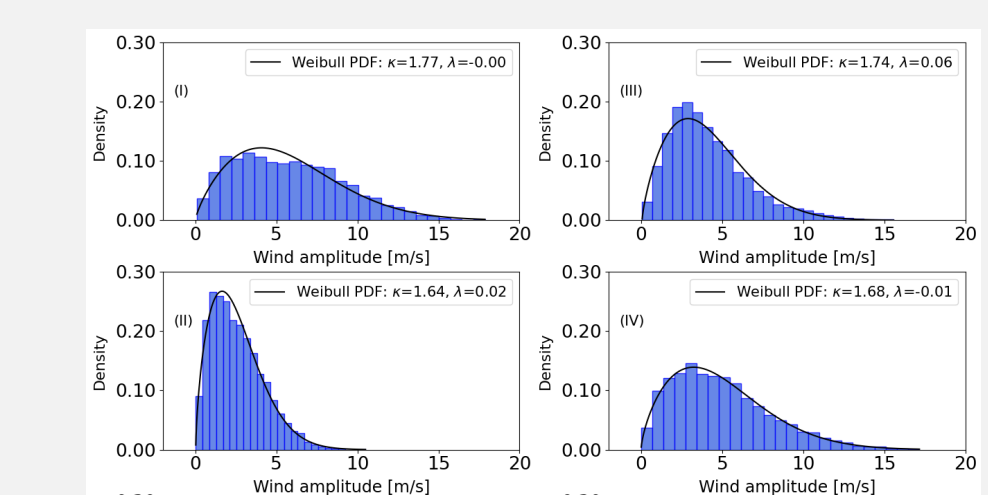
**Skew-normal PDF fit on wind components (U, V)**



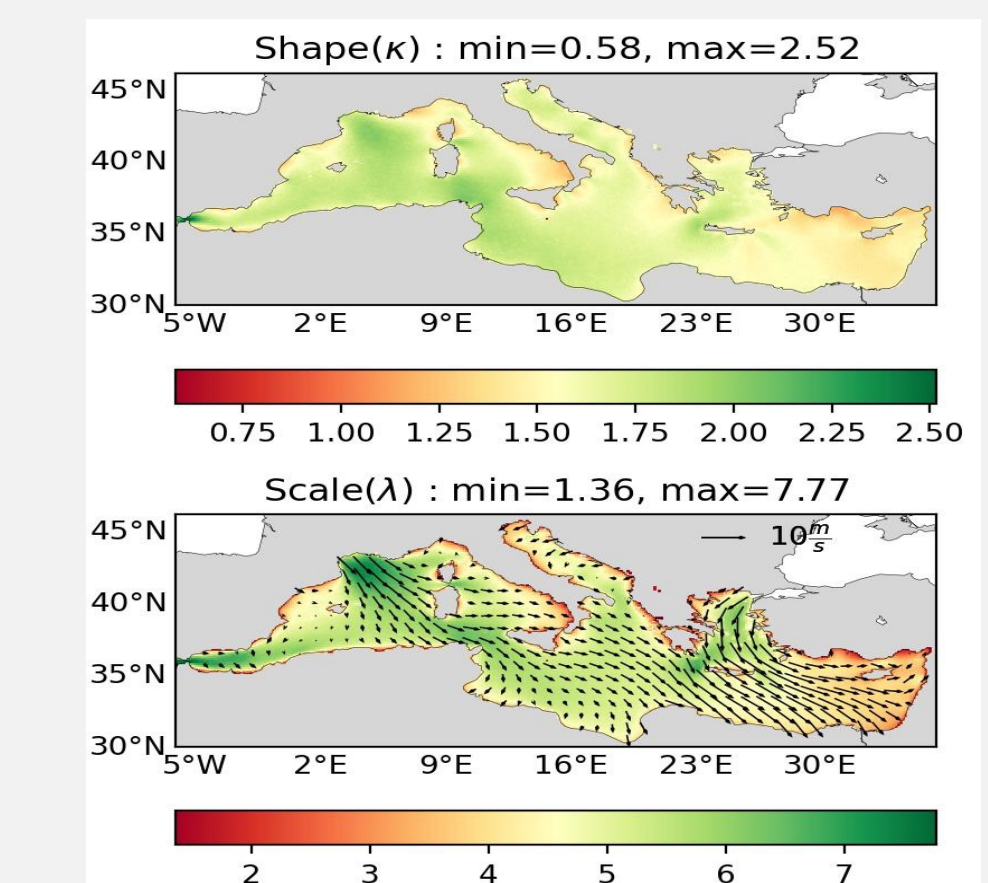
The single grid point distributions for wind (U, V): (i) Alboran Sea (ii) Gulf of Lion (iii) Adriatic Sea (iv) Ionian sea



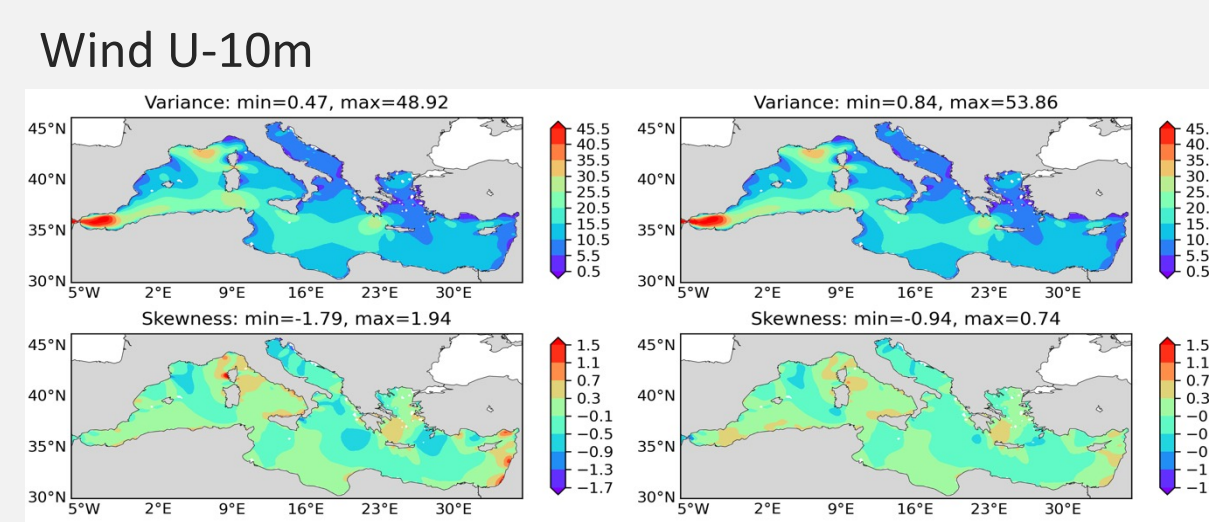
Shape, location and scale parameter distribution for wind-U-10m and wind-V-10m



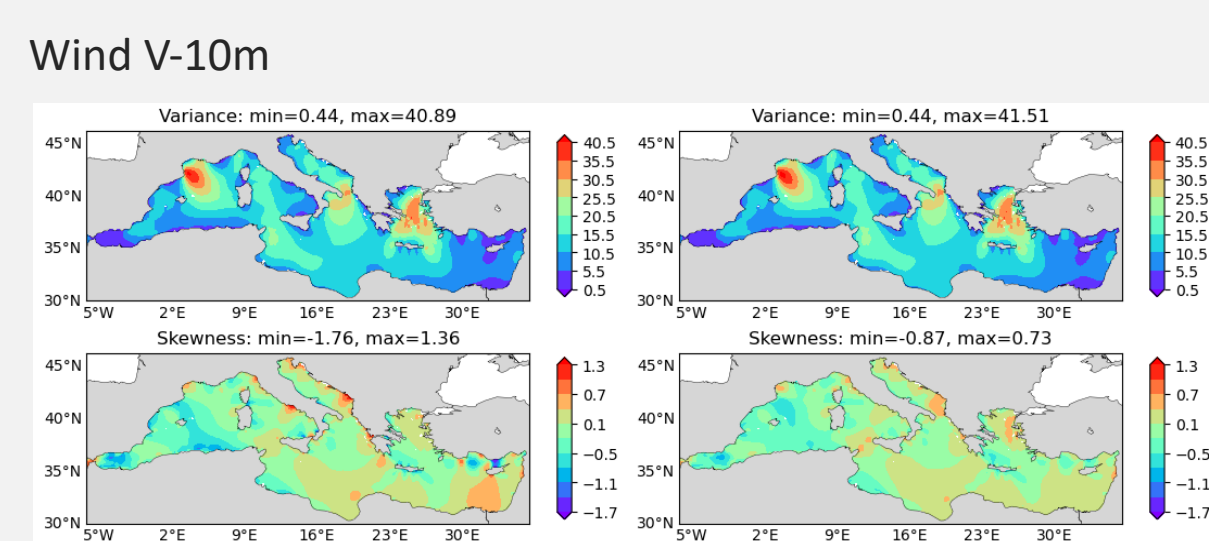
The single grid point distributions for W: (i) Alboran Sea, (ii) Gulf of Lion (iii) Adriatic Sea (iv) Ionian Sea



Shape and location parameter for wind amplitude (W)

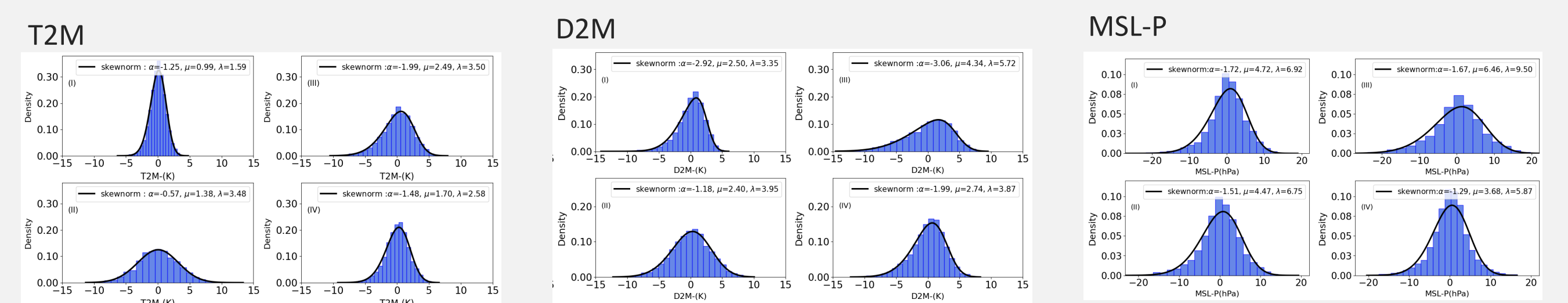


Distributions of the statistical moments (variance and skewness) estimated from data and skew-normal fitted distributions [Up: Wind-U10m, Bottom: Wind-V10m]

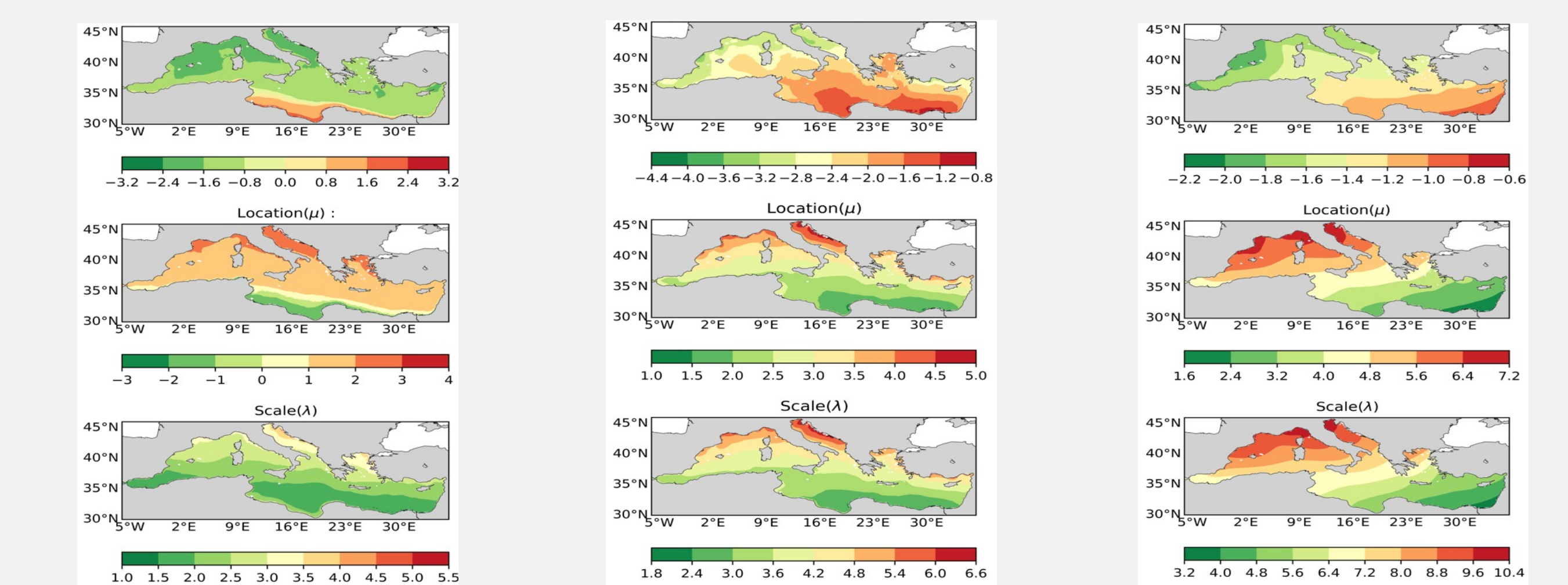


Distributions of the statistical moments (variance and skewness) estimated from data and skew-normal fitted distributions [Up: Wind-U10m, Bottom: Wind-V10m]

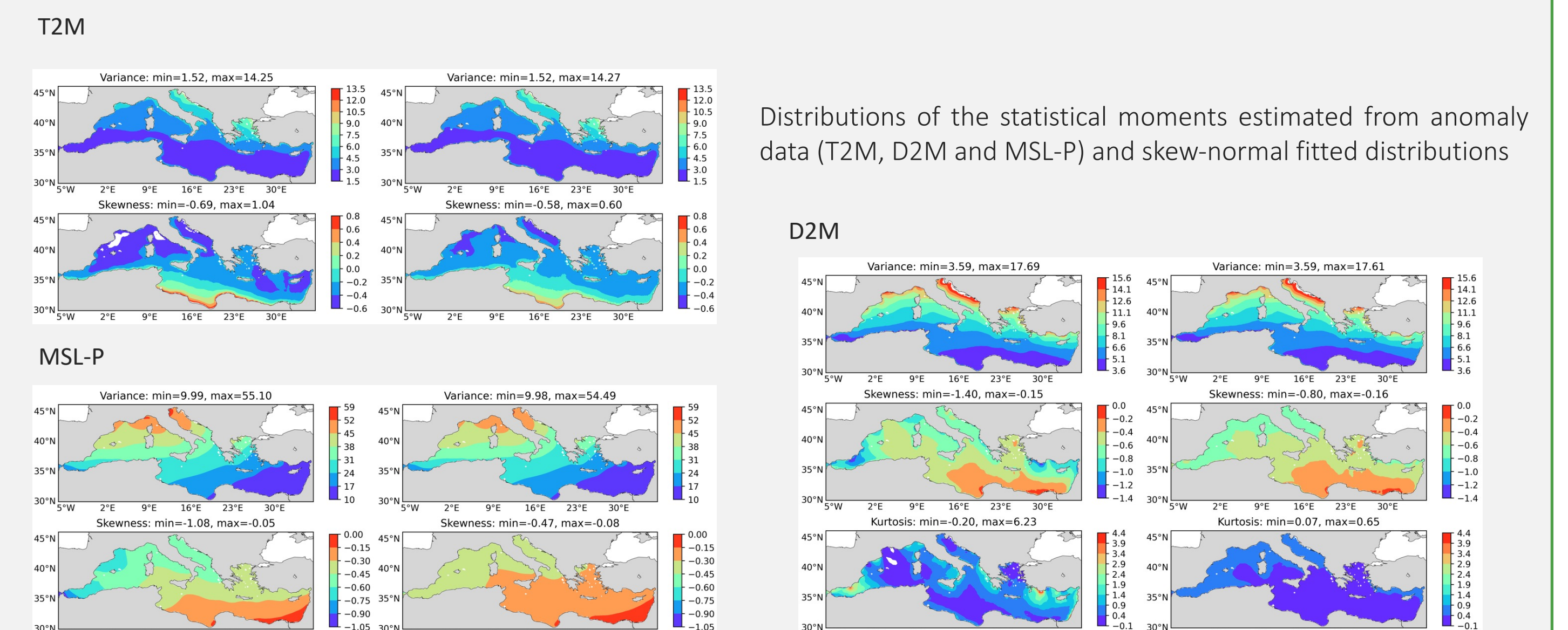
**Skew-normal PDF fit on T2M, D2M and MSL-P**



The Single grid point histograms for T2M, D2M and MSL-P: (i) Alboran Sea (ii) Gulf of Lion (iii) Adriatic Sea (iv) Ionian Sea



Distributions of shape, location and scale parameter of T2M (left), D2M (middle) and MSL-P (right)



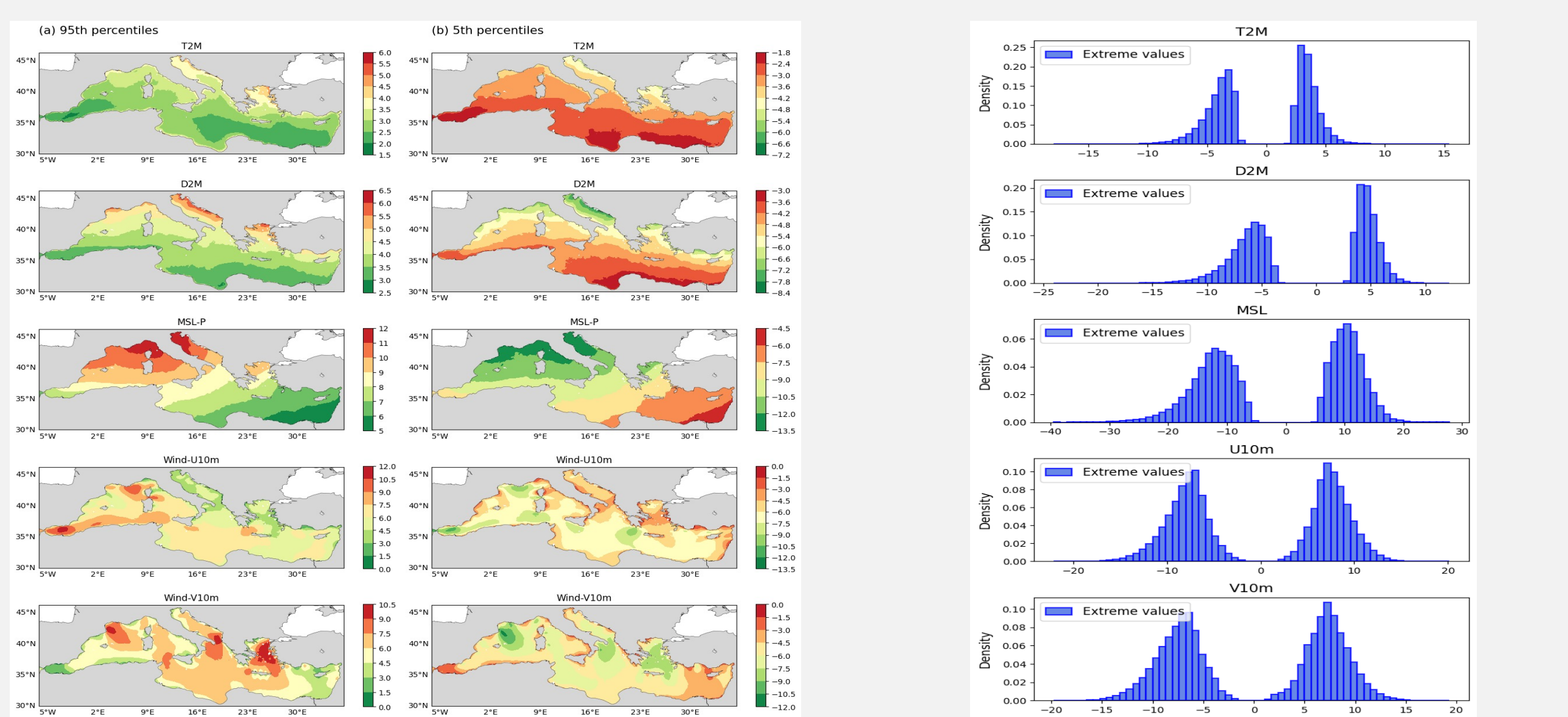
Distributions of the statistical moments estimated from anomaly data (T2M, D2M and MSL-P) and skew-normal fitted distributions

**Potential Extremes**

Percentile values are computed from the estimated PDFs at each grid point using the inverse Cumulative Density Function (CDF).

$$f(x; \alpha, \mu, \lambda) = \Phi\left(\frac{x-\mu}{\lambda}\right) - 2T\left(\frac{x-\mu}{\lambda}, \alpha\right) \dots\dots\dots(6)$$

Where,  $\Phi(z)$  is the CDF of a normal distribution and  $T(z; \alpha)$  auxiliary function related to skewness parameter  $\alpha$



95th percentile (or 0.95 quantile) and 05th percentile (or 0.05 quantile) value distributions of selected atmospheric variables

Histograms of combined 95th percentile (or 0.95 quantile) and 5th percentile (or 0.05 quantile) excluding normal range

**Conclusions**

- Weibull PDF is confirmed to be the correct PDF for wind amplitude over all the Mediterranean Sea
- The skew-normal PDF is instead emerging as a potential best fit PDF for wind (U, V) components, T2M, D2M and MSL-P.
- Skewness for all the variables is moderate with large differences across the Mediterranean region with the largest skewness values in the Northern Mediterranean Sea areas
- The extreme values show a significant difference between the northern and southern Mediterranean, especially for T2M, D2M and MSL-P, with the latter a contrast between the western and eastern Mediterranean
- Potential extremes are concentrated mainly in Alboran Sea, Gulf of Lion, Adriatic Sea and Aegean Sea

**References**

• Ghani, M.H, F. Trota, S. Bianconcini, G.Liguori, N.Pinardi, 2024. Modeling the surface atmospheric variables distributions in the Mediterranean Sea. (Submitted)  
• Azzalini, A. (1985). A class of distributions which includes the normal ones. *Scandinavian journal of statistics*, 171-178.  
• Peter C. Chu. (2009). "Statistical Characteristics of the Global Surface Current Speeds Obtained from Satellite Altimetry and Scatterometer Data". In: IEEE Journal of selected topics in applied Earth observations and remote sensing, Vol. 2, no. 1 (2009).